

Important Integration formula

- $\int \frac{1}{\sqrt{1-x^2}} dx = \sin^{-1} x + C$
- $\int \frac{1}{1+x^2} dx = \tan^{-1} x + C$
- $\int \frac{1}{|x|\sqrt{x^2-1}} dx = \sec^{-1} x + C$
- $\int \sin^n(x) dx = \frac{-1}{n} \sin^{n-1}(x) \cos(x) + \frac{n-1}{n} \int \sin^{n-2}(x) dx$
- $\int \cos^n(x) dx = \frac{1}{n} \cos^{n-1}(x) \sin(x) + \frac{n-1}{n} \int \cos^{n-2}(x) dx$
- $\int \tan^n(x) dx = \frac{1}{n-1} \tan^{n-1}(x) - \int \tan^{n-2}(x) dx$
- $\int \sec^n(x) dx = \frac{1}{n-1} \sec^{n-2}(x) \tan(x) + \frac{n-2}{n-1} \int \sec^{n-2}(x) dx$
- $\int \csc^n(x) dx = \frac{-1}{n-1} \csc^{n-2}(x) \cot(x) + \frac{n-2}{n-1} \int \csc^{n-2}(x) dx$

Basic integration formula

$$\int x^n = x^{n+1}/n+1 + C$$

$$\int \cos x = \sin x + C$$

$$\int \sin x = -\cos x + C$$

$$\int \sec^2 x = \tan x + C$$

$$\int \operatorname{cosec}^2 x = -\cot x + C$$

$$\int \sec x \tan x = \sec x + C$$

$$\int \operatorname{cosec} x \cot x = -\operatorname{cosec} x + C$$

$$\int dx/\sqrt{1-x^2} = \sin^{-1} x + C$$

$$\int dx/\sqrt{1-x^2} = -\cos^{-1} x + C$$

$$\int dx/\sqrt{1+x^2} = \tan^{-1} x + C$$

$$\int dx/\sqrt{1+x^2} = -\cot^{-1} x + C$$

$$\int e^x = e^x + C$$

$$\int a^x = a^x / \log a + C$$

$$\int dx/x\sqrt{x^2-1} = \sec^{-1} x + C$$

$$\int dx/x\sqrt{x^2-1} = \operatorname{cosec}^{-1} x + C$$

$$\int 1/x = \log |x| + c$$

$$\int \tan x = \log |\sec x| + c$$

$$\int \cot x = \log |\sin x| + c$$

$$\int \sec x = \log |\sec x + \tan x| + c$$

$$\int \operatorname{cosec} x = \log |\operatorname{cosec} x - \cot x| + c$$

Some Special Function Integrals

$$\int dx/(x^2 - a^2) = 1/2a \log |(x-a)/(x+a)| + c$$

$$\int dx/(a^2 - x^2) = 1/2a \log |(a+x)/(a-x)| + c$$

$$\int dx/(x^2 + a^2) = 1/a \tan^{-1} x/a + c$$

$$\int dx/\sqrt{x^2 - a^2} = \log |"x" + \sqrt{x^2 - a^2}| + C$$

$$1. \int dx/\sqrt{a^2 - x^2} = \sin^{-1} x/a + c$$

$$\int dx/\sqrt{x^2 + a^2} = \log |"x" + \sqrt{x^2 + a^2}| + C$$

Definite Integration Properties

$$P_0: \int_a \rightarrow b f(x) dx = \int_a \rightarrow b f(t) dt$$

$$P_1: \int_a \rightarrow b f(x) dx = -\int_b \rightarrow a f(x) dx. \text{ In particular, } \int_a \rightarrow a f(x) dx = 0$$

$$P_2: \int_a \rightarrow b f(x) dx = \int_a \rightarrow c f(x) dx + \int_c \rightarrow b f(x) dx$$

$$P_3: \int_a \rightarrow b f(x) dx = \int_a \rightarrow b f(a + b - x) dx.$$

$$P_4: \int_0 \rightarrow a f(x) dx = \int_0 \rightarrow a f(a - x) dx$$

$$P_5: \int_0 \rightarrow 2a f(x) dx = \int_0 \rightarrow a f(x) dx + \int_0 \rightarrow a f(2a - x) dx$$

$$P_6: \int_0 \rightarrow 2a f(x) = \left\{ \begin{array}{l} 2 \int_0 \rightarrow a f(x) dx, \text{ if } f(2a - x) = f(x) \\ \int_0 \rightarrow a f(x) dx - \int_0 \rightarrow a f(x) dx, \text{ if } f(2a - x) = -f(x) \end{array} \right.$$

$$P_7: \int(-a) \rightarrow a f(x) = \left\{ \begin{array}{l} 2 \int_0 \rightarrow a f(x) dx, \text{ if } f(-x) = f(x) \\ -2 \int_0 \rightarrow a f(x) dx, \text{ if } f(-x) = -f(x) \end{array} \right.$$